

2 Design, Modeling and Optimization of an 3 Ocean Wave Power Generation Buoy

4 AUTHORS

5 **Carlos Velez**

6 Department of Mechanical
7 and Aerospace Engineering,
8 University of Central Florida

9 **Zhihua Qu**

10 Department of Electrical
11 Engineering and Computer Science,
12 University of Central Florida

13 **Kuo-Chi Lin**

14 Department of Mechanical
15 and Aerospace Engineering,
16 University of Central Florida

17 **Shiyuan Jin**

18 Department of Electrical
19 Engineering and Computer Science,
20 University of Central Florida

42 ABSTRACT

43 Ocean waves provide an abundant, clean, and renewable source of energy. Exist-
44 ing systems, typically hydraulic turbines powered by high-pressure fluids, are very
45 large in size and costly. Additionally, they require large ocean waves in which to op-
46 erate. This paper details the design, development, and laboratory prototype testing of
47 a wave power generation system comprising a buoy that houses a set of mechanical
48 devices and a permanent magnetic generator. The buoy, floating on the surface of the
49 ocean, utilizes the vertical movement of ocean waves to pull on a chain anchored to
50 the ocean floor. The linear motion is translated into rotation, which rotates a shaft to
51 move armature coils within the generator to produce an electric current. The amount
52 of energy generated increases with wave height and input frequency. The flywheel
53 inertia, shaft rotation speed, and electrical load are optimized to provide maximize
54 electricity production. The paper addresses the design, analysis, and implementation
55 of mechanical and electrical systems, together with resistive load control, system op-
56 timization, and performance analysis. Both simulation and experimental results are
57 provided and compared.

58 **Keywords:** buoy, ocean wave energy, permanent magnetic generator, load control,
59 wave power generation

21 Introduction

22 **R**esearch into safe and clean energy
23 harvesting from renewable sources has
24 become popular in response to the
25 current energy crisis and growing en-
26 vironmental awareness. Renewable en-
27 ergy sources principally include solar,
28 wind, hydroelectric, ocean waves, etc.
29 Wind and solar power are restricted
30 to specific geographic regions; wind
31 power is only useful in windy areas,
32 and solar power is effective in only
33 sunny ones. Ocean wave power is espe-
34 cially promising because more than
35 two thirds of the Earth's surface is cov-
36 ered by ocean, which should allow wise
37 access across the globe. Nature offers
38 large amounts of kinetic energy in the
39 form of ocean waves, and it is esti-
40 mated that if 0.2% of the untapped
41 energy of the ocean could be harvested,

60 it could provide power sufficient for the
61 entire world (Falnes, 2002).

62 This paper presents the novel design,
63 development, and laboratory prototype
64 testing of the wave power generation
65 system, shown in Figure 1, in which a
66 set of mechanical devices and a perma-
67 nent magnetic generator are installed
68 inside a buoy. The buoy floats on the
69 surface of the ocean and utilizes the ver-
70 tical movement of ocean waves to gen-
71 erate electric power. Specifically, when
72 the buoy moves from the trough to
73 the crest, the buoyancy force and hydro-
74 dynamic force pull upon the chain an-
75 chored to the ocean floor and rotates
76 the shaft to move armature coils of the
77 generator to produce electricity; mean-
78 while, the coiled spring in the reel is
79 pulled and tightened. Similarly, when
80 the buoy moves from the crest to the

81 trough, the reel rewinds the cable, and
82 the system returns to its original state.

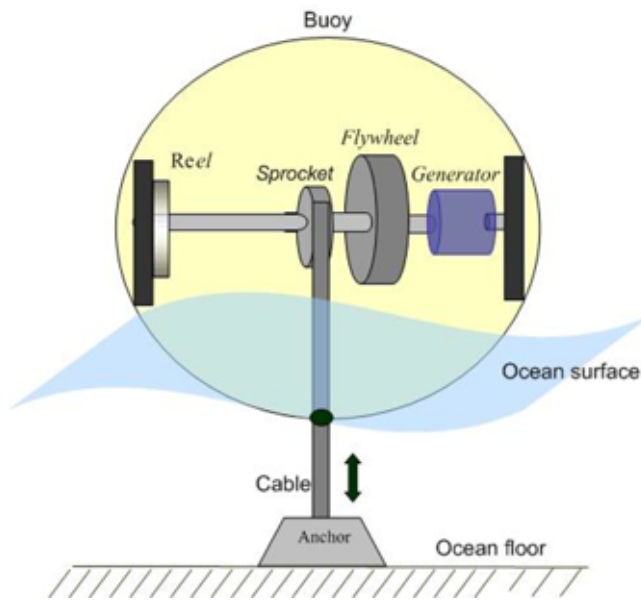
83 The project thus far can be broken
84 into three stages:

- 85 1. Before implementing the labora-
86 tory prototype, a Matlab simulation
87 was used to simulate the hydro-
88 dynamics and the mechanical and
89 electrical models. The simulation
90 process aided the optimization of
91 the system's electric power output.
- 92 2. Next, the laboratory prototype was
93 constructed and selected data were
94 measured.
- 95 3. Finally, the prototype results were
96 analyzed. Laboratory prototype data
97 were compared with simulation data
98 and identified discrepancies were
99 analyzed.

100 This design incorporates many tech-
101 nically challenging components such

FIGURE 1

Conceptual design, wave power generation.



dynamics, mechanical engineering, in addition to control and power systems. There is much to improve in system efficiency, cost, reliability, and scalability to make the extraction of wave energy practical for consumer use. A few typical wave energy development examples are listed below.

- Conceptual Wave Park by Oregon State University (Brekken et al., 2009): OSU is the pioneer in research and development of wave energy in the United States. It is reported that a network of about 500 buoys could power the business district of downtown Portland. Its linear generator using linear translational motion harvests energy from one directional motion of a buoy.
- JAMSTEC, Japan (Osawa et al., 2002): This system contains three air chambers that convert wave energy into pneumatic energy. Wave action causes the internal water level in each chamber to rise and fall, forcing a bidirectional airflow over an air turbine. The turbines drive three induction generators to produce a three-phase AC output at 200 Volts. More research has been done by Cunha et al. (2009), Elwood et al. (2010), Haniotis et al. (2002), Kimoulakis et al. (2008), Leijon et al. (2005), Mueller and Baker (2002), Rhinefrank et al. (2006), and Wolfbrandt (2006).

These systems all share the same difficulty in converting the oscillatory motion of waves to the rotation of a permanent magnet generator. The proposed concept utilizes a buoy to convert its linear height displacement into electrical energy. The vertical displacement of the buoy will enable a chain to rotate the shaft of a generator installed within the buoy itself. Through the use of a pulley system,

102 as the wet-dry interface of the cable, 129
103 mooring design, hazardous environ- 130
104 mental effects such as biofouling, 131
105 and multidirectional buoy motion. 132
106 These components are needed for 133
107 field installation but are not currently 134
108 considered as they are outside the 135
109 scope of this theoretical mechanical 136
110 study. The objective of this paper is 137
111 to study and optimize solely the in- 138
112 ternal mechanical components within 139
113 the buoy for a one-dimensional oscil- 140
114 lating wave motion. System optimi- 141
115 zation was done by integrating the 142
116 hydrodynamic model along with the 143
117 mechanical and electric models. Ad- 144
118 ditionally, load control was applied
119 to vary the electrical load on the out-
120 put of the generator and to regulate the
121 rotor rpm in the case of irregular wave
122 motion.

123 The remainder of the paper is or-
124 ganized as follows:

- 125 ■ Existing Wave Power Genera-
126 tion Technologies introduces exist-
127 ing ocean wave power generation
128 technologies.

- 129 ■ Laboratory Prototype Design intro-
130 duces conceptual and laboratory
131 prototype designs.
- 132 ■ Mathematical Model provides the
133 mathematical equations and theo-
134 retical analysis.
- 135 ■ System Optimization addresses sys-
136 tem optimization (including simu-
137 lation and prototyping test results).
- 138 ■ Results and Discussion provides
139 experimental results and discussion
140 of voltage output, tension measure-
141 ment, RPM, and electrical power
142 output.
- 143 ■ Conclusion concludes the paper.

Existing Wave Power Generation Technologies

145 Compared with other forms of gen-
146 eration of electricity such as wind and
147 hydro power, research on wave energy
148 is still in its infancy. Wave energy
149 development is a field that requires
150 multidisciplinary, cooperative efforts
151 including technologies in hydro-

the rotation of the generator shaft will be amplified with respect to the actual buoy displacement. Incorporating these components will lead to a small, inexpensive, light-weight and consistent form of producing energy for the applications including the powering of nearby coastal regions or offshore platforms.

Laboratory Prototype Design

The prototype mechanical system has been designed and constructed and can convert the kinetic energy developed from the heaving forces generated by ocean waves into electrical energy. The internal mechanism of the buoy is designed to translate the vertical oscillations of a buoy into rotational energy that will power a generator. Figure 2 is a snapshot of wave power generation system inside the buoy.

Mechanical Components

In Figure 2, a single long chain wraps around two sets of sprockets on the rotor shaft (connected to the generator) and then loops downward and is wrapped around two rotational

bearings fixed to the laboratory floor. There are two loops made by a single chain connecting the moving rotor with the fixed rotor. This double loop design multiplies the chain velocity at the second loop/sprocket by a factor of 4. Additionally, the double loop design allows for unidirectional rotation of the main rotor (shown in Figure 2) independent of the direction of motion of the chain/buoy. In effect, even if the buoy is oscillating up and down, it will only incur a clockwise directional torque on the generator shaft. In order for the chain to loop around and drive the rotor shaft, two sprockets are required. The first sprocket is located at the first chain loop where clockwise rotation will drive the rotor; during counter-clockwise rotation, it will spin freely around the main rotor. The second sprocket is located where the chain loops around the rotor for the second time. This sprocket is reversed and operates opposite to the first sprocket. When the buoy moves upward, the first sprocket drives the generator and the second sprocket spins freely. The opposite is true for the downward motion of the buoy, resulting in unidirectional rotation of the rotor with bidirectional motion of the buoy/chain. One end of the chain

is attached to a constant torque rotational spring, which acts to keep tension in the chain, and the other end of the chain is fixed to the moving buoy. This rotational spring also helps drive the shaft in order to ensure the continued rotation of the shaft. The shaft is coupled to a permanent magnet generator, which extracts power from the rotating motion of the shaft. To increase the inertia of the shaft assembly, three steel flywheels are fastened onto the driven shaft.

In order to test the performance of the mechanical system, a 6-DOF motion table is utilized to simulate the motion of a wave. The motion of the platform is prescribed to follow a sinusoidal path in the vertical direction only. The mechanism is placed on top of the platform with the chain fixed to the floor, simulating a mooring to the ocean floor. The platform was programmed to move at various frequencies ranging from 0.1 to 0.3 Hertz and at amplitudes of 5–15 cm.

Electrical Components

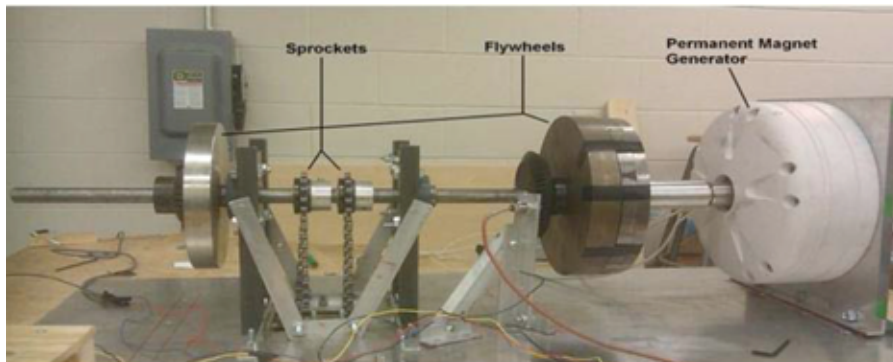
In order to analyze the performance of the mechanism, several parameters were measured during the experiments.

- An optical sensor was used to measure the instantaneous RPM of the shaft.
- A potentiometer was used to measure the instantaneous location of the platform.
- A strain gauge was placed on one of the links in the chain in order to constantly measure tension in the chain.
- A Data Acquisition Board (DAQ) measured the power output from the generator; the three leads of the generator are brought out and connected to a diode rectifier.

A program constructed in LABVIEW controlled a relay switch.

FIGURE 2

Prototype wave generation system.



312 The relay switch position is dependent
 313 on the shaft RPM and position of the
 314 platform. When load is applied, the
 315 load current flows inside the generator,
 316 inducing a voltage drop across the
 317 internal circuit resistance. Applying
 318 additional resistance increases the
 319 torque of the generator, thereby reduc-
 320 ing the RPM.

321 Design Issues Regarding 322 Optimal Performance

323 Components within the mechani-
 324 cal system can be optimized to im-
 325 prove overall system performance.
 326 The optimal performance is intended
 327 to produce the largest amount of
 328 power, while preventing the system
 329 from experiencing any large peak
 330 or cyclical stresses that would greatly
 331 limit the life span of the mechanism.

332 The amount of inertia contributed
 333 by the flywheels is one simple way to
 334 optimize the efficiency of the system.
 335 By increasing the inertia of the shaft,
 336 one raises the potential energy in
 337 the rotating shaft. Consequently, the
 338 torque needed to rotate the shaft at
 339 a set RPM is increased because of the
 340 increase in inertia. The proper amount
 341 of shaft inertia is determined by the
 342 size of the ocean waves, and this will
 343 subsequently drive the dimensions of
 344 the buoy. Additionally a gear train
 345 may be implemented to convert excess
 346 torque into an increased RPM of the
 347 shaft; increasing the gear ratio will pro-
 348 portionally increase the shaft speed.
 349 Thus, the gear ratio should be opti-
 350 mized to increase the RPM of the
 351 shaft while not limiting the motion
 352 of the buoy too much through the in-
 353 crease in mass. The dimensions of the
 354 sprockets can also be optimized to im-
 355 prove the performance of the overall
 356 system. Reducing the radius of the
 357 sprocket increases the shaft RPM and
 358 reduces the amount of torque created

359 by the buoy. The method in which
 360 the generator extracts energy from
 361 the rotating shaft can be selected to
 362 conserve the momentum of the fly-
 363 wheels. Varying the electrical resis-
 364 tance or load on the generator can
 365 allow one to control the required torque
 366 needed to drive the generator. A de-
 367 tailed analytical solution is developed
 368 to optimize the system components
 369 and is addressed at the optimization
 370 section of this paper.

371 Mathematical Model 372 Laboratory Prototype Model

373 The system can be represented by
 374 three models: hydrodynamic model,
 375 generator motion model, and buoy
 376 model, as illustrated in Figure 3.

377 The relationship between mechan-
 378 ical and electrical torques and angular
 379 acceleration can be represented by the
 380 following equation:

$$381 \quad T_m - T_e = I \frac{d\omega}{dt} \quad (1)$$

382 where T_m is the mechanical torque, T_e
 383 is the electromagnetic back-torque, I is
 384 the moment of inertia of the system,
 385 and ω is the angular velocity of the
 386 shaft. The mechanical torque is created
 387 by both the tension from the tethered

387 cable as well as system frictional force.
 388 The electrical torque is developed by
 389 the rotor of the generator as it rotates
 390 in the magnetic field with a resistive
 391 load applied to the generator.

392 Hydrodynamic Model

393 The ocean wave motion is trans-
 394 ferred into rotational motion for the
 395 permanent magnetic generator via the
 396 motion imparted on the floating buoy.
 397 Wave forces consist of both rotational
 398 and heaving forces. In this paper, only
 399 the one-dimensional heaving force is
 400 considered in the hydrodynamic
 401 model. The equation of motion is
 402 modeled by the following:

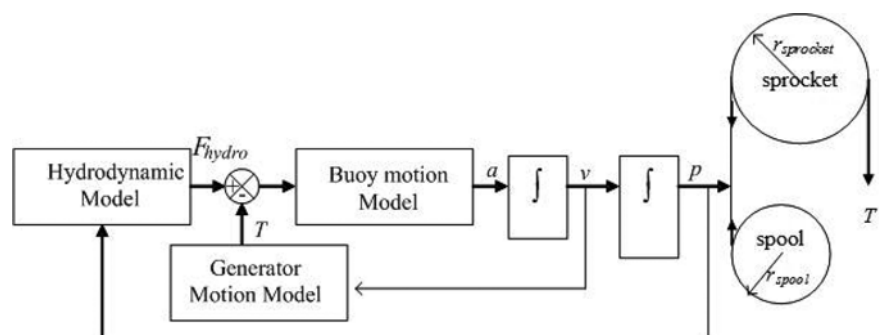
$$403 \quad m\ddot{z} = F_b + F_{excite} - F_{drag} - mg - T \quad (2)$$

404 where m is the total mass of the buoy
 405 including all components inside it, z is
 406 the vertical displacement of the buoy,
 407 F_B is the buoyance force acting on
 408 the buoy, F_{excite} is the vertical wave
 409 excitation force which is described
 410 shortly, F_{drag} is the hydrodynamic
 411 drag force acting on the buoy, and T
 412 is the tension force of the cable which
 413 tethers the buoy to ocean floor (Sarpkaya
 414 & Isaacson, 1981). F_B , F_{drag} , T , and
 415 F_{excite} can be calculated as follows.

$$416 \quad F_b = \rho_w g V_{submerged} \quad (3)$$

381 **FIGURE 3**

382 Hydrodynamic and buoy system model.



415 where w is the water density and $V_{submerged}$ is the submerged volume of the buoy.
 416 When a spherical buoy is in hydrostatic equilibrium, the weight of the buoy is bal-
 417 anced by the buoyancy force. Assuming that the water level reaches a height of y_0
 418 above the center of the sphere, then the overall static buoyancy force experienced
 419 by the buoy is governed by the following equation

$$F_b = \rho_w g \left[\frac{2}{3} \pi R^3 + \pi \left(R^2 y_0 - \frac{1}{3} y_0^3 \right) \right] \quad (4)$$

420 where ρ_w is the density of the water (displaced fluid) and R is the radius of the spher-
 421 ical buoy.

422 Next, the drag force (F_D) in equation (2) is expressed analytically as

$$F_{drag} = -\frac{1}{2} \rho_w C_d A_b |\dot{z}| \dot{z} \quad (5)$$

423 where C_d , set to 0.75, is the drag coefficient of the buoy and A_b is the area of the
 424 submerged surface of the buoy projected on a plane normal to the z -direction. The
 425 drag coefficient, C_d , is a function of the geometry of the buoy and the Reynolds
 426 number of the fluid, but for convenience purposes it will be modeled as a constant
 427 for this paper (Leonard et al., 2000). The drag force contributes the least of the five
 428 forces due to its low velocity (\dot{z}).

429 The cable tension force (T) in equation (2) is expressed as

$$T = T_o + D_{coupled} * \left(C_{load} * \frac{C_{gen} \omega}{r} + \frac{I \alpha}{r} \right)$$

$$C_{load} = \begin{cases} 1 & \text{if load is on} \\ 0 & \text{if otherwise} \end{cases}$$

$$D_{coupled} = \begin{cases} 1 & \text{Coupled} \\ 0 & \text{Uncoupled} \end{cases} \quad (6, 7, 8)$$

430
 431
 432 where C_{load} represents the electrical load state, C_{gen} is the generator back-torque
 433 coefficient (generation load), $D_{coupled}$ represents the coupled/uncoupled state of
 434 the mechanical system discussed shortly, α is the angular acceleration of the
 435 shaft, and r is the radius of the sprocket.

436 The last force in equation (2) is the wave excitation force. The excitation
 437 force of a wave acting on a body can be separated into three components: the
 438 Froude-Krylov force, the diffraction force, and the radiation force (Patel, 1989).
 439 The Froude-Krylov force, realized as wave momentum, is imparted onto a sub-
 440 merged body, and the diffraction and radiation forces come from the disturbances
 441 to the surrounding fluid. The size of the buoy was considered significantly smaller
 442 than the length of the surface waves; as a result, the diffraction and radiation forces
 443 were considered negligible. Thus, the wave excitation force is equated to the Froude-
 444 Krylov force, as detailed below:

$$F_{excite} = -\rho_w \iint \frac{d\Phi_i}{dt} \hat{n} dS_{submerged} \quad (9)$$

445 In the above equation, the surface in-
 446 tegral is taken over the submerged
 447 surface of the buoy. The normal vec-
 448 tor to the surface is denoted by \hat{n} ;
 449 since the simulation investigates
 450 one-dimensional motion, only the
 451 z -component of the normal vector is
 452 used.

453 Equations (4)–(9) can be com-
 454 bined together into equation (2) to cre-
 455 ate the governing equation of motion.
 456 It is impractical to solve analytically;
 457 instead numerical methods are used
 458 to calculate the position, velocity, and
 459 acceleration of the buoy at each time-
 460 step. The resulting data can be used to
 461 determine the RPM of the shaft, the
 462 tension in the cable, and the expected
 463 power output for a given generator
 464 model (C_{gen}).

465 In order to simulate the system as
 466 accurately as possible, it is necessary
 467 to analyze the system in three separate
 468 stages.

- 469 ■ **Stage I:** Decoupled stage (upper
 470 half of upstroke)—On the upper
 471 half of upstroke, the buoy deacceler-
 472 ates. The sprocket decouples from
 473 the shaft, that is, the angular veloc-
 474 ity of the shaft exceeds that of the
 475 sprocket; the pulling force of the
 476 buoy cable does not contribute
 477 work to the flywheel. Only the res-
 478 istive force of the generator and
 479 friction exert forces on the shaft.
- 480 ■ **Stage II:** Down-stroke stage—On
 481 the down-stroke, there is no pulling
 482 force at the cable tethered in the
 483 buoy. The resistive load force of
 484 the generator is not applied as well,
 485 for the consideration of load con-
 486 trol to keep flywheel momentum
 487 which forces the system to run con-
 488 tinuously, although the frictional
 489 force (is proportional to angular ve-
 490 locity) slows the shaft.
- 491 ■ **Stage III:** Coupled stage (lower half
 492 of upstroke)—On the low half of

493 upstroke, the pulling force/torque
494 accelerates the system until to the
495 equilibrium point when the angular
496 velocity of the shaft no longer in-
497 creases. In addition to the pulling
498 force, the resistive force of the gen-
499 erator and friction force also apply
500 to the shaft, countering the pulling
501 force/torque. The maximum ten-
502 sion is applied right after the lowest
503 turning point.
504

505 Generator Model

506 The simulation of the system inte-
507 grated the hydrodynamic force of the
508 buoy into the mechanical and electrical
509 models. For the experimental portion
510 of this project, a GL-PMG-500A per-
511 manent magnet generator, manufac-
512 tured by Ginlong Technologies, Inc.,
513 was utilized. This model has the ad-
514 vantage of a low start up torque (due
515 to low cogging and resistive torque
516 design) and high efficiency. The resis-
517 tor load in this experiment is 1:6,
518 which matches the resistive load tested
519 by the generator's manufacturer. Ac-
520 cording to the generator specification,
521 the power output can be represented as
follows:

$$522 P = \frac{\left(\frac{w * 60}{2\pi}\right)^2}{16.6} \quad (10)$$

523 where w is the RPM of the shaft.

523 System Optimization

524 As mentioned previously, given a
525 fixed wave amplitude and frequency,
526 the optimal power output P_{max} de-
527 pends on several factors. The radius
528 of sprocket, r , the inertia of the fly-
529 wheel(s), I , the ratio of the gear set
530 used, GR , and the controlled electrical
531 load added to the generator, L , may be

532 adjusted to increase the power out-
533 put of the system. The objective is to
534 choose values for these parameters
535 from their feasible ranges in an optimal
536 way in order to get maximum power
537 output. Of course the optimum values
538 are dependent on the design of the
539 buoy, and even more importantly,
540 the wave conditions; the result is that
541 in order to achieve truly optimum out-
542 put, the parameters would have to
543 dynamically adjust based on the con-
544 stantly changing wave conditions.
545 This is impractical, and instead the
546 design parameters should be optimized
547 based on the estimated average wave
548 characteristics.

549 Matlab Simulation

550 A simulation was run in Matlab to
551 determine the estimated power output
552 using the one-dimensional scheme de-
553 tailed in the previous section. In order
554 to solve the differential equation given
555 in equation (2), a fourth-order, explicit
556 Runge-Kutta algorithm was imple-
557 mented. The simulation is executed
558 for a 60-s duration with a time-step
559 of 0.05 s; initial conditions of dynamic
560 equilibrium was imposed. The buoy is
561 modeled simply as a sphere of radius R
562 and the surface wave is a perfect sinu-
563 soid. Each design parameter may be
564 adjusted independently within the
565 simulation so as to determine the effect
566 on the power output. The average power
567 output is given for the 60-s simulation
568 and used for comparison. Table 1 de-
569 tails the values of all of the constants
570 used within the Matlab simulation.

571 The Matlab simulation is capable
572 of outputting the instantaneous values
573 of several system variables, including
574 the tension in the mooring cable, the
575 RPM of the shaft, and the generator
576 output power. The simulation is run
577 utilizing the inputs given in Table 1
578 (except for a 20-s duration).

579 The simulation is useful for pre-
580 dicting the average power output for
581 given system inputs. Because the sim-
582 ulation uses arbitrary values for the
583 parameters to be optimized, the results
584 of this method are only suboptimal.
585 To determine the actual optimal val-
586 ues, all parameters need to be varied
587 simultaneously. For simplicity, only
588 three design parameters are inves-
589 tigated here: flywheel inertia (I), the
590 gear ratio (GR), and the load control
591 threshold (L).

592 Flywheel Inertia 593 Optimization

594 Without adequate inertia on the
595 shaft, the flywheel may not continu-
596 ously rotate throughout the complete
597 wave cycle. With excessive inertia, on
598 the other hand, the angular accelera-
599 tion of the shaft will suffer as a result
600 of increased chain tension, as seen in
601 equations (6) and (2). As such, the in-
602 ertia of the shaft should be optimized
603 so that the motion of the shaft is con-
604 tinuous while limiting the effect on
605 the buoy motion. Given a fixed wave
606 amplitude and frequency, reasonable
607 flywheel inertia can be chosen to max-
608 imize electrical power output. The
609 value of the shaft inertia is varied in
610 the Matlab simulation for values be-
611 tween 0.05 and 0.5 kg m²; with in-
612 crements of 0.01 kg m². The power
613 output corresponding to the peak
614 power is a function of the other param-
615 eters, but for the given inputs the op-
616 timal inertia for the shaft is found to
617 be 0.25 kg m².

618 Gear Ratio Optimization

619 The generator detailed in the simu-
620 lation is relatively small, with a low
621 back-torque coefficient and ideal shaft

TABLE 1

Simulation parameter values for the optimization model.

Parameter	Value	Description
A_w	1	Amplitude of wave [m]
F	0.2	Frequency of wave [1/s]
R	0.5	Radius of buoy [m]
m	200	Mass of buoy [m]
ρ_w	997.0	Density of water at 25 °C [kg/m ³]
μ	0.001	Dynamic viscosity of water at 25 °C [kg/ms]
C_d	0.45	Drag coefficient of sphere [unit-less]
g	9.81	Gravitational acceleration [m/s ²]
T_o	100	Spool tension [kg m/s ²]
T_{fin}	60	Duration of model [s]
δt	0.02	Time step for model [s]
C_{gen}	6.36	Back-torque coefficient [kg $\frac{m^2}{s}$]
β_{fric}	0.5	Mechanical friction coefficient [kg m ² /s]
T_{start}	5	Start-up torque for generator [kg m/s ²]
I	0.1	Moment of Inertia of system [kg m ²]
GR	1.0	Gear ratio [unit-less]
L	0	Load control threshold [RPM]
R	0.05	Radius of sprocket [m]

input of around 275 RPM. To achieve this ideal speed, the gear ratio is likely to be on the order of, but greater than, unity. In the Matlab simulation, the gear ratio is a multiplier acting on the speed of the shaft and it acts to transmit the resulting large back-torques to the tension of the mooring line, as detailed in equation (6). The gear ratio is varied from 0.5 to 5, with increments of 0.1 in the simulation. Figure 4 illustrates the relationship between GR and the resulting average power output for the system.

Electrical Load Control Optimization

By adjusting the timing at which the load is applied, continuous power extraction may be sacrificed in order

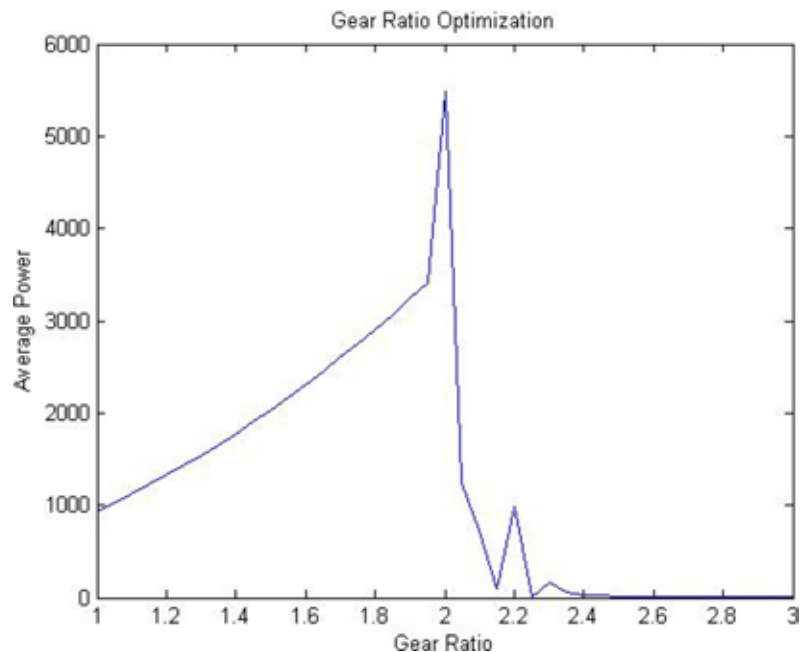
to prevent the shaft from slowing to a standstill. Intuition suggests that the load should be applied while the shaft RPM is high above some threshold, and it should be disconnected while it becomes low. Furthermore, the electrical load should be controlled such that:

1. least load is applied in the down stroke when there is no wave force and
2. the oscillating velocity of the system is in phase with the wave's excitation force acting on the system (Kimoulakis & Kladas, 2008).

Usually the oscillating velocity of the buoy is out of phase with the wave's excitation force. Therefore, to maximize the electrical output power, the electrical load should be controlled in a way to make the buoy operate synchronously with the wave. The implementation of load control can be enhanced by selecting a threshold for which the load is disengaged. For

FIGURE 4

Electrical power output vs. gear ratio.



667 example, if the RPM of the shaft
668 drops below the threshold the load
669 is reduced and then reengaged when
670 the RPM rises above it. This load
671 control threshold (LC) was a param-
672 eter in the Matlab simulation and
673 varied from 0 to 200 RPM, at incre-
674 ments of 5 RPM. The suboptimal
675 value for the load control threshold
676 is found to be 170 RPM. Using this
677 point as the threshold value, the elec-
678 trical load is disconnected from the
679 generator when the shaft speed falls
680 below 170 RPM.

681 Optimization of the 682 Sprocket Radius

683 The radius of the sprocket is di-
684 rectly related to the shaft RPM. The
685 smaller the radius, the greater the
686 RPM, but this also increases chain
687 tension. The simulation did not dem-
688 onstrate a clear relationship between
689 sprocket size and power output; it ap-
690 peared that the smaller the sprocket
691 radius, the greater the power. It may
692 be possible that a very small sprocket
693 would provide an optimum size, but
694 this would be impractical. Instead,
695 the chosen sprocket is the smallest,
696 commercially available unit that is suf-
697 ficiently large enough to support the
698 stresses induced by the peak chain
699 tension.

700 Overall System Optimization

701 The suboptimal values found for
702 the flywheel inertia, gear ratio, and
703 the load control threshold are not
704 very useful by themselves because
705 of the arbitrary selection of values for
706 the other parameters. To find the ac-
707 tual optimal values, all three parameters
708 must be optimized simultaneously to
709 account for system interdependencies.
710 The three suboptimal values may serve
711 as guidelines for where to inspect each
712 of the parameters for the actual opti-

713 mal values. For instance, when
714 running the overall optimization simu-
715 lation, values near 0.25 kg m^2 inertia,
716 2.0 gear ratio, and 170 RPM load
717 threshold should be investigated
718 as one or more may lie close to the
719 actual system's optimum. The system
720 scheme was done by brute force, a
721 range around each of the aforemen-
722 tioned values was selected, and each
723 scenario with that range was inspected
724 to determine the highest power out-
725 put. This method is effective, but
726 highly inefficient. Nevertheless, opti-
727 mum values were discovered for the
728 given inputs for the defined buoy sys-
729 tem and wave characteristics. The op-
730 timal parameters resulted in an inertia
731 of 0.18 kg m^2 , a gear ratio of 2.2, and
732 load control of 190 (RPM).

733 Results and Discussion 734 Simulated Wave

735 In the laboratory prototype test,
736 an electrical 6-DOF motion system is
737 used to mimic the movement of ocean
738 waves. The motion system consists of
739 a motion platform, a base frame, a
740 motion control cabinet, and a mo-
741 tion computer that can simulate the
742 very complicated movements (i.e., a
743 combination of lateral and vertical
744 movements) of a buoy. Figure 1 is a
745 simplified view of wave power genera-
746 tion system concept. All mechanical
747 assemblies including the generator
748 (shown at the upper right corner) are
749 mounted to the motion platform. A
750 chain is routed through a hole in the
751 platform, and one end is attached to
752 a pull-box directly tethered to the
753 ground. The other end is fixed to the
754 moving table. When the platform
755 moves up, it pulls the chain to run
756 over the sprockets to rotate the shaft;
757 when the platform moves down, the
758 pull-box tightens the chain.

667 Sensor Devices 668 and Measurements

669 In the laboratory prototype testing,
670 the following sensors are used to per-
671 form measurements to aide in opti-
672 mizing the system. A strain gauge is
673 used to measure the tension in the
674 chain. This measurement is important
675 in the design of the buoy to reduce the
676 probability of a chain breaking due
677 to excessive stress. An RPM encoder
678 is used to measure the instantaneous
679 RPM of the flywheel and generator.
680 A displacement sensor is attached to
681 the motion platform to measure the
682 instantaneous height of the platform.
683 This sensor is used in conjunction
684 with a relay switch to automatically
685 apply the electrical load at the most
686 potent sections of the up-strokes.

687 Measurement of Voltage, 688 Load Control, and RPM

689 The measurement of voltage, load
690 control, and RPM under a frequency
691 of 0.3 Hz and amplitudes (platform
692 movement) of 10 cm and 12 cm were
693 performed. After calculation, the av-
694 erage power output under the ampli-
695 tude of 10 cm was 113.37 W. At
696 an input amplitude of 12 cm, the sys-
697 tem generated 136.13. Shaft RPMs
698 were 188.60 and 221.42, respectively.
699 This results in a 17.40% increase
700 in RPM and a 20.08% increase in
701 power (W) for experiments run with
702 a flywheel with moment of inertia
703 of 0.10 kg m^2 .

704 A Comparison of Simulation 705 and Experimental Results

706 Comparisons (RPM and power
707 output) were made between the
708 Matlab simulation and laboratory
709 prototype results, at the same input
710 torque; that is, the input torque based
711 on the measured tension force in the

prototype was used as the input torque to the Matlab simulation model.

Figure 5 shows the RPM data from both the simulation and the prototype unit. The experimental RPM is not smooth as the platform moves down; however, both datasets show similar patterns—RPMs increase quickly as the platform moves up and decrease slowly as the platform moves downward, a direct effect of the load control. When the RPM drops below the set threshold, the relay switch turns off, decreasing the electrical load. The momentum of the flywheels engages, and the shaft RPM decreases slowly as the energy stored in the flywheel momentum is depleted. Compared with the experimental results, the RPM in the simulation model drops more quickly at the beginning in the downstroke and then decays more slowly. It should be noted that the electrical load (its resistive torque) is much greater than the frictional torque in the mechanical system.

Several factors can cause the observed discrepancies. For example, it is difficult to measure the friction of the mechanical system or accurately

simulate the generator model and its resistive torque. Furthermore, the motion platform can create a sinusoidal movement similar to a wave, but it is difficult to mimic the complex hydrodynamic buoy model, which includes several, more complex forces.

Conclusion

This paper introduces an innovative design, development, and laboratory prototype of a light-weight, low-cost, small-size wave power generation system which includes a buoy, a set of mechanical devices, and a permanent magnetic generator. Prior to prototype setup, a hydrodynamic model, buoy model, and a generator model were analyzed, and a Matlab system simulation was conducted. The flywheel inertia, shaft rotation speed, and electrical load are optimized to maximize electricity production. The current laboratory prototype is capable of generating an average of 136 W under the movement of a motion platform with 12 cm in amplitude, 0.3 Hz frequency, and 0.10 kg m² moment of inertia, and 206 W with 10 cm in

amplitude, 0.3 Hz frequency, and 0.25 kg m² moment of inertia. System performance regarding the mechanical power input and electrical output was analyzed based on experimental data such as tension of the chain, shaft RPM, and voltage output. Both simulation and experimental results are provided and compared to verify the laboratory prototype design with reasonable correlation between them. The success of this mechanical system and optimized design could promise a clean, safe, and abundant energy source to satisfy a significant portion of society's energy needs in the future.

Corresponding Author:

Carlos Velez

Department of Mechanical and Aerospace Engineering,

University of Central Florida

4000 Central Florida Boulevard,

Orlando, FL 32826

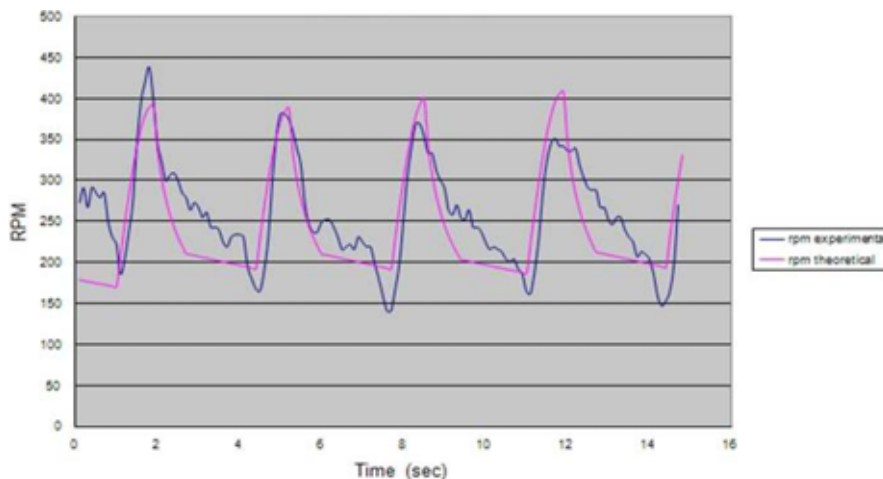
Email: velezcar@yahoo.com

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FIGURE 5

Comparison of RPM from Matlab simulation and prototype experimentation.



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